

## Weld Joint Design Equations and Calculations

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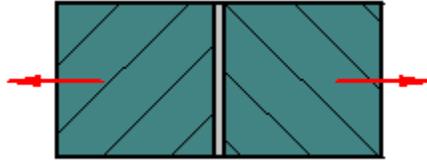
## Spot Weld Design Equations and Calculations

- [Spot Weld Single-Shear Load Stress Equation and Calculation](#)
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## Welding Types and Processes

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## [Weld Design Menu](#)



### Normal Stress

$$\sigma_1 = \frac{F_n}{A} \quad [\text{MPa, psi}]$$

Where :

$\sigma_1$  = Normal stress [MPa,psi]

$F_n$  = Normal force [N, lb]

$A$  = Throat area of weld [ $\text{mm}^2$ ,  $\text{in}^2$ ]

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### Reference Stress

$$\sigma_5 = \frac{\sigma_1}{\alpha_1} \quad [\text{MPa, psi}]$$

Where:

$\sigma_5$  = Reference stress [MPa,psi]

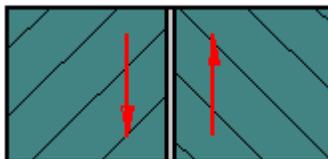
$\sigma_1$  = Normal stress [MPa,psi]

$\alpha_1$  = Coefficient of weld joint

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### Weld Design Menu



### Shear Stress

$$\tau = \frac{F_t}{A} \quad [\text{MPa, psi}]$$

**Where :**

$\tau$  = Shear stress [MPa,psi]

$F_t$  = shear force [N, lb]

$A$  = Throat area of the weld [ $\text{mm}^2$ ,  $\text{in}^2$ ]

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### Reference Stress

$$\sigma_s = \frac{\tau}{\alpha_2} \quad [\text{MPa,psi}]$$

**Where :**

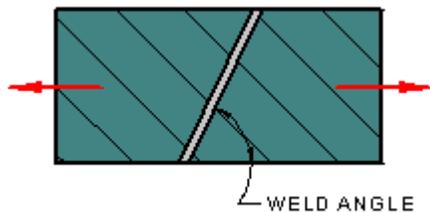
$\sigma_s$  = Reference stress [MPa , psi]

$\tau$  = Shear stress [MPa, psi]

$\alpha_2$  = Coefficient of weld joint

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### Weld Design Menu



### Normal Stress

$$\sigma = \frac{F \cdot \cos \delta}{A} \quad [\text{MPa,psi}]$$

**Where :**

$\sigma$  = Normal Stress [MPa,psi]

$F$  = Acting force [N, lb]

$\delta$  = Weld angle [ $\diamond$ ]

$A$  = Throat area of the weld [ $\text{mm}^2$ ,  $\text{in}^2$ ]

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### Shear Stress

$$\tau = \frac{F \cdot \sin \delta}{A} \quad [\text{MPa, psi}]$$

**Where :**

$\tau$  = Shear Stress [MPa,psi]

$F$  = Acting force [N, lb]

$\delta$  = Weld direction angle [°]

$A$  = Throat area of the weld [mm<sup>2</sup>, in<sup>2</sup>]

### Resultant reduced stress

$$\sigma_R = \sqrt{\sigma^2 + 3 \cdot \tau^2} \quad [\text{MPa, psi}]$$

**Where:**

$\sigma_R$  = Resultant Reduced Stress [MPa,psi]

$\sigma$  = Normal stress [MPa,psi]

$\tau$  = Shear stress [MPa,psi]

### Reference Stress

$$\sigma_S = \sqrt{\left(\frac{\sigma}{\alpha_1}\right)^2 + 3 \cdot \left(\frac{\tau}{\alpha_2}\right)^2} \quad [\text{MPa, psi}]$$

**Where:**

$\sigma_S$  = Reference Stress [MPa,psi]

$\sigma$  = Normal stress [MPa,psi]

$\tau$  = Shear stress [MPa,psi]

$\alpha_1, \alpha_2$  = Coefficients of the weld joint

### Weld Design Menu

#### Resultant Reduced Stress

$$\sigma_R = \sqrt{(\sigma_1 + \sigma_2 + \sigma_3)^2 + 3 \cdot (\tau)^2} \quad [\text{MPa, psi}]$$

**Where:**

$\sigma_R$  = Resultant Reduced Stress [MPa,psi]

$\sigma_1, \sigma_2,$  = Normal stress [MPa,psi]

$\tau$  = Shear stress [MPa,psi]

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### Reference Stress

$$\sigma_s = \sqrt{\left(\frac{\sigma_1 + \sigma_2 + \sigma_3}{\alpha_1}\right)^2 + 3 \cdot \left(\frac{\tau}{\alpha_2}\right)^2} \quad [\text{MPa,psi}]$$

Where :

$\sigma_s$  = Reference Stress [MPa, psi]

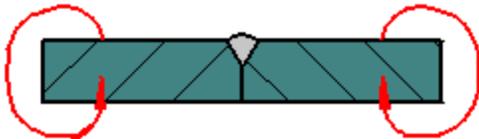
$\sigma_1, \sigma_2, \sigma_3$  = Normal Stress [MPa,psi]

$\tau$  = Shear stress [MPa,psi]

$\alpha_1, \alpha_2$  = Coefficient of weld joint

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### Weld Design Menu



### Shear Stress

$$\tau_{\max} = \frac{u \cdot T}{W} \quad [\text{MPa,psi}]$$

Where :

$\tau_{\max}$  = Shear Stress [MPa,psi]

**u** = constant

- for calculation in metric units  $u = 1000$

- for calculation in imperial units  $u = 12$

**T** = torque [Nm, lb-ft]

**W** = section modulus of throat area of the weld [ $\text{mm}^3, \text{in}^3$ ]

## Reference Stress

$$\sigma_5 = \frac{\tau_{\max}}{\alpha_2} \quad [\text{MPa,psi}]$$

Where :

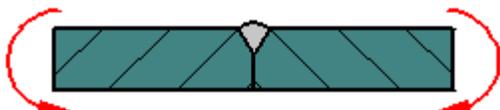
$\sigma_5$  = Reference Stress [MPa,psi]

$\alpha_2$  = Shear Stress [MPa,psi]

$\tau_{\max}$  = coefficient of the weld joint

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## Weld Design Menu



## Normal Stress

$$\sigma_3 = \frac{u \cdot M_2}{W} \quad [\text{MPa,psi}]$$

Where :

$\sigma_3$  = Normal stress [MPa,psi]

$u$  = Constant

- for calculation in metric units  $u = 1000$

- for calculation in imperial units  $u = 12$

$M_2$  = Bending moment [Nm, lb-ft]

$W$  = Section modulus of throat area of weld [ $\text{mm}^3$ ,  $\text{in}^3$ ]

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## Reference Stress

$$\sigma_5 = \frac{\sigma_3}{\alpha_1} \quad [\text{MPa,psi}]$$

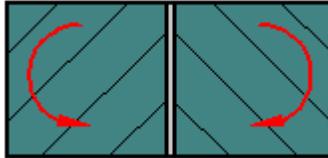
Where:

$\sigma_5$	= Reference stress [MPa,psi]
$\sigma_3$	= Normal stress [MPa,psi]

$\alpha_1$  = Coefficient of weld joint

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## Weld Design Menu



### Normal Stress

$$\sigma_2 = \frac{u \cdot M_1}{W} \quad [\text{MPa, psi}]$$

Where :

$\sigma_2$  = Normal stress [MPa,psi]

$u$  = Constant

- for calculation in metric units  $u = 1000$

- for calculation in imperial units  $u = 12$

$M_1$  = Bending moment [Nm, lb ft]

$W$  = Section modulus of throat area of the weld [ $\text{mm}^3$ ,  $\text{in}^3$ ]

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### Reference Stress

$$\sigma_s = \frac{\sigma_2}{\alpha_1} \quad [\text{MPa, psi}]$$

Where:

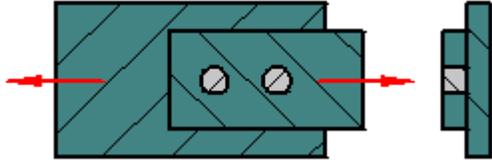
$\sigma_s$  = Reference stress [MPa,psi]

$\sigma_2$  = Normal stress [MPa,psi]

$\alpha_1$  = Coefficient of weld joint

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## Weld Design Menu



### Shear Stress in Weld Base Area

$$\tau_z = \frac{F}{0.5 \cdot d^2 \cdot i} \quad [\text{MPa, psi}]$$

Where:

- $\tau_z$  = Shear stress in weld base area [MPa,psi]
  - F = Shear force [N, lb]
  - d = Diameter of plug weld [mm,in]
  - i = Number of welds
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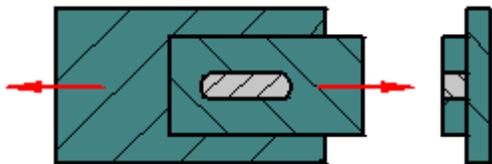
### Shear Stress in Weld Peripheral Area

$$\tau_o = \frac{F}{2.2 \cdot d \cdot s \cdot i} \quad [\text{MPa, psi}]$$

Where:

- $\tau_o$  = Shear stress in weld peripheral area [MPa,psi]
  - F = Shear force [N, lb]
  - d = Diameter of plug weld [mm,in]
  - s = Plate thickness [mm, in]
  - i = Number of welds
- 

## [Weld Design Menu](#)



### Shear Stress in Weld Base Area

$$\tau_z = \frac{F}{0.7 \cdot b \cdot L \cdot i} \quad [\text{MPa, psi}]$$

**Where:**

- $\tau_z$  = Shear stress in weld base area [MPa,psi]
  - F = Shear force [N, lb]
  - b = Width of weld [mm,in]
  - L = Length of weld [mm,in]
  - i = Number of welds
- 

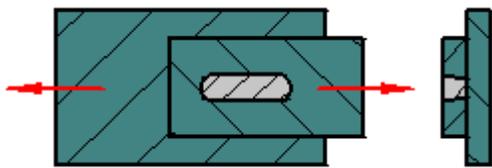
### Shear Stress in Weld Peripheral Area

$$\tau_o = \frac{F}{1.4 \cdot s \cdot L \cdot i} \quad [\text{MPa, psi}]$$

**Where:**

- $\tau_o$  = Shear stress in weld peripheral area [MPa,psi]
  - F = Shear force [N, lb]
  - s = Plate thickness [mm, in]
  - L = Length of weld [mm,in]
  - i = Number of welds
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### Weld Design Menu



### Shear Stress in Weld Base Area

$$\tau_z = \frac{F}{b \cdot L \cdot i} \quad [\text{MPa, psi}]$$

**Where:**

- $\tau_z$  = Shear stress in weld base area [MPa,psi]
- F = Shear force [N, lb]
- b = Width of weld [mm,in]

L = Length of weld [mm,in]  
i = Number of welds

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### Shear Stress in Weld Peripheral Area

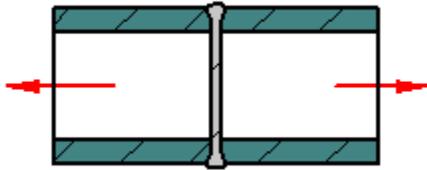
$$\tau_o = \frac{F}{2 \cdot s \cdot L \cdot i} \quad [\text{MPa,psi}]$$

Where:

$\tau_o$  = Shear stress in weld peripheral area [MPa,psi]  
F = Shear force [N, lb]  
s = Plate thickness [mm, in]  
L = Length of weld [mm,in]  
i = Number of welds

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### Weld Design Menu



### Normal Stress in Weld Base Area

$$\sigma = \frac{F_z}{A} \quad [\text{MPa,psi}]$$

Where:

$\sigma$  = Normal stress [MPa,psi]  
 $F_z$  = Applied axial force [N, lb]  
A = Throat area of weld [mm<sup>2</sup>,in<sup>2</sup>]

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### Comparative Stress

$$\sigma_s = \frac{\sigma}{\alpha_1} \quad [\text{MPa,psi}]$$

Where:

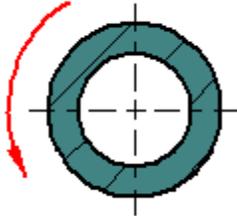
$\sigma_s$  = Comparative stress [MPa,psi]

$\sigma$  = Normal stress [MPa,psi]

$\alpha_1$  = Conversion coefficient of weld joint

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### Weld Design Menu



#### **Circumference Butt Weld Stress with Torque Shear Stress**

$$\tau = \frac{u \cdot T}{W} \quad [\text{MPa, psi}]$$

#### **Where:**

$\tau$  = Shear stress [MPa,psi]

u = Constant

Metric units u=1000

Imperial units u=12

W = Section modulus throat area [ $\text{mm}^3$ ,  $\text{in}^3$ ]

T = Torque applied [Nm, lb-ft]

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#### **Comparative Stress**

$$\sigma_s = \frac{\tau}{\alpha_2}$$

#### **Where:**

$\sigma_s$  = Comparative stress [MPa,psi]

$\tau$  = Shear stress [MPa,psi]

$\alpha_2$  = Conversion coefficient of weld joint

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### Weld Design Menu

#### **Circumference Butt Weld Stress with Combined Shear and Axial Loading**

## Resultant Reduced Stress

$$\sigma_R = \sqrt{\sigma^2 + 3 \cdot \tau^2} \quad [\text{MPa,psi}]$$

### Where:

$\sigma_R$  = Resultant seduced stress [MPa,psi]

$\sigma$  = Normal Stress [MPa,psi]

$\tau$  = Shear Stress [MPa,psi]

## Comparative Stress

$$\sigma_S = \sqrt{\left(\frac{\sigma}{\alpha_1}\right)^2 + 3 \cdot \left(\frac{\tau}{\alpha_2}\right)^2} \quad [\text{MPa,psi}]$$

### Where:

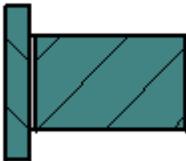
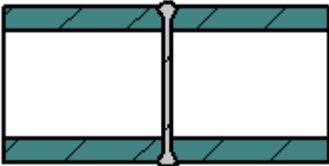
$\sigma_S$  = Comparative stress [MPa,psi]

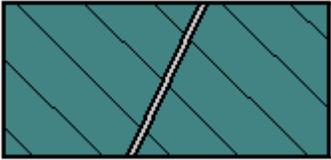
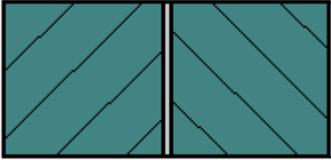
$\sigma$  = Normal stress [MPa,psi]

$\tau$  = Shear stress [MPa,psi]

$\alpha_1, \alpha_2$  = Conversion coefficient of weld joint

## Weld Design Menu

Butt Weld Orientation	Weld Illustration	Throat Area of Butt Weld [mm <sup>2</sup> , in <sup>2</sup> ]	
		Full Weld Length	Active Load-bearing Length
Butt End Tube Weld		$A = s L$	$A = s (L - 2 s)$
Circumferential Tube Weld		$A = \pi s (d - s)$	$A = s (L - 2 s)$

Angled Relative to applied load		$A = s \cdot \frac{L}{\cos \delta}$	$A = s \cdot \left( \frac{L}{\cos \delta} - 2 \cdot s \right)$
Normal to Applied Load		$A = s L$	$A = s (L - 2 s)$

**Where:**

A = Area in<sup>2</sup>

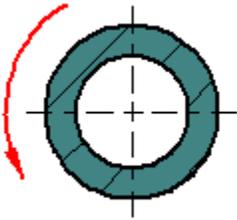
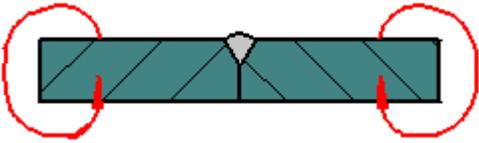
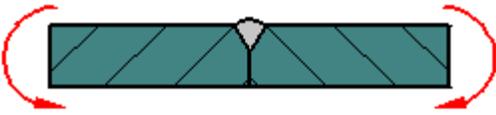
$\delta$  = Weld angle [deg]

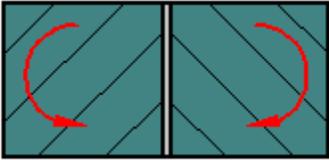
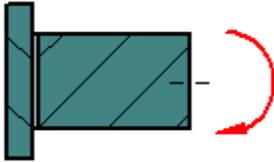
s = Plate or tube thickness [mm, in]

L = Length of weld [mm, in]

$\pi$  = pi (3.14157)

### Weld Design Menu

Weld Illustration	Section Modulus of Throat Area of Butt Weld [mm <sup>3</sup> , in <sup>3</sup> ]	
	Full Weld Length	Active Load-bearing Length
	$W = \frac{\pi}{2} \cdot s \cdot (D - s)^2$	$W = \frac{s \cdot (L - 2 \cdot s)^2}{6}$
	$W = \frac{s^2 \cdot L^2}{3 \cdot L + 1.8 \cdot s}$	$W = \frac{s^2 \cdot (L - 2 \cdot s)^2}{3 \cdot (L - 2 \cdot s) + 1.8 \cdot s}$
	$W = \frac{s^2 \cdot L}{6}$	$W = \frac{s^2 \cdot (L - 2 \cdot s)}{6}$

	$W = \frac{\pi}{2} \cdot s \cdot (D - s)^2$	$W = \frac{s \cdot (L - 2 \cdot s)^2}{6}$
	$W = \frac{s \cdot L^2}{6}$	

**Where:**

- W = Section modulus [mm<sup>3</sup>, in<sup>3</sup>]
- s = Plate or tube thickness [mm, in]
- L = Length of weld [mm, in]
- $\pi$  = pi (3.14157)

### Weld Design Menu

Weld	Polar Moment of Inertia	
	Fillet "J" Weld [mm <sup>4</sup> , in <sup>4</sup> ]	Location Center of Gravity
	$J = a \cdot \frac{L^3}{12}$	$\bar{X} = \frac{L}{2} \quad \bar{Y} = 0$
	$J = a \cdot \left( \frac{(H+B)^4 - 6 \cdot H^2 \cdot B^2}{12 \cdot (H+B)} \right)$	$\bar{X} = \frac{B^2}{2 \cdot (H+B)} \quad \bar{Y} = 0$
	$J = a \cdot \left( \frac{H \cdot (3 \cdot B^2 + H^2)}{6} \right)$	$\bar{X} = \frac{B^2}{2 \cdot (H+B)} \quad \bar{Y} = 0$
	$J = a \cdot \left( \frac{H \cdot (3 \cdot B^2 + H^2)}{6} \right)$	$\bar{X} = \frac{B}{2} \quad \bar{Y} = 0$
	$J = a \cdot \left( \frac{(8 \cdot B^3 + 6 \cdot B \cdot H^2 + H^3)}{12} - \frac{B^4}{2 \cdot B + H} \right)$	$\bar{X} = \frac{B^2}{2 \cdot B + H} \quad \bar{Y} = 0$
	$J = a \cdot \left( \frac{(8 \cdot H^3 + 6 \cdot H \cdot B^2 + B^3)}{12} - \frac{H^4}{2 \cdot H + B} \right)$	$\bar{X} = \frac{B}{2} \quad \bar{Y} = 0$

	$J = a \cdot \frac{(H+B)^3}{16}$	$\bar{X} = \frac{B}{2}$ $\bar{Y}$
	$J = 2 \pi a (r + a/2)^3$	-
	$J = a \cdot \left( \frac{H^3 + B^3}{6} + \frac{B \cdot H^2}{2} \right)$ $J = a \cdot \left( \frac{(H - 2 \cdot t)^3 + 3 \cdot (H - 2 \cdot t) \cdot s^2 + B^3 + 3 \cdot B \cdot H^2}{6} \right)$	-
	$J = a \cdot \left( \frac{B^3 + 2 \cdot H^3}{6} + H \cdot B^2 \right)$ $J = a \cdot \left( \frac{B^3 + 2 \cdot H^3 - s^3}{6} + H \cdot B^2 + \frac{B \cdot s^2 - s \cdot B^2}{2} - 2 \cdot (H - s) \cdot (B \cdot t - t^2) \right)$	-
	$J = a \cdot \left( \frac{H^3 + B^3}{6} + \frac{H \cdot B^2}{2} \right)$ $J = a \cdot \left( \frac{(B - 2 \cdot t)^3 + 3 \cdot (B - 2 \cdot t) \cdot s^2 + H^3 + 3 \cdot H \cdot B^2}{6} \right)$	-

**Where:**

- J = Polar Moment of inertia [mm<sup>4</sup>, in<sup>4</sup>]
- $\bar{X}$  = Center of Gravity Location [mm, in]
- $\bar{Y}$  = Center of Gravity Location [mm, in]
- A = Height fillet weld [mm, in]
- B = Width of weld [mm, in]
- s = Web thickness [mm, in]
- L = Length of weld [mm, in]
- r = Weld radius [mm, in]
- t = Flange thickness [mm, in]
- H = Height of fillet weld group [mm, in]

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**[Weld Design Menu](#)**

Weld	Moment of Inertia	
	Fillet "I" Weld [mm <sup>4</sup> , in <sup>4</sup> ]	Location Center of Gravity
	$I = a \cdot \frac{L^3}{12}$	$\bar{Y} = \frac{L}{2}$
	$I = a \cdot \frac{H^3}{6}$	$\bar{Y} = \frac{H}{2}$
	$I = a \cdot \frac{B \cdot H^2}{2}$	$\bar{Y} = \frac{H}{2}$
	$I = a \cdot \frac{(6 \cdot B + H) \cdot H^2}{12}$	$\bar{Y} = \frac{H}{2}$
	$I = a \cdot \left( \frac{2 \cdot H^3}{3} - 2 \cdot \bar{Y} \cdot H^2 + (B + 2 \cdot H) \cdot \bar{Y}^2 \right)$	$\bar{Y} = \frac{H^2}{2 \cdot H + B}$
	$I = a \cdot \frac{(3 \cdot B + H) \cdot H^2}{6}$	$\bar{Y} = \frac{H}{2}$
	$I = \pi a (r + a/2)^3$	-
	$I = a \cdot \frac{(3 \cdot B + H) \cdot H^2}{6}$ $I = a \cdot \left( \frac{(H - 2 \cdot t)^2}{6} + \frac{B \cdot H^2}{2} \right)$	$\bar{Y} = \frac{H}{2}$
	$I = a \cdot \left( \frac{2 \cdot H^3}{3} - 2 \cdot \bar{Y} \cdot H^2 + (B + 2 \cdot H) \cdot \bar{Y}^2 \right)$ $I = a \cdot \left( \frac{(H - t)^3}{6} + 2 \cdot H \cdot \left( \frac{H + t}{2} - \bar{Y} \right)^2 + B \cdot \bar{Y}^2 \right)$	$\bar{Y} = \frac{H^2}{2 \cdot H + B}$ $\bar{Y} = \frac{H^2 - t^2}{2 \cdot H + B - 2 \cdot t}$
	$I = a \cdot \left( \frac{2 \cdot H^3}{3} - 2 \cdot \bar{Y} \cdot H^2 + 2 \cdot (B + H) \cdot \bar{Y}^2 \right)$ $I = a \cdot \left( \frac{2 \cdot H^3}{3} - 2 \cdot \bar{Y} \cdot H^2 + 2 \cdot (B + H) \cdot \bar{Y}^2 - B \cdot t \cdot (2 \cdot \bar{Y} - t) \right)$	$\bar{Y} = \frac{H^2}{2 \cdot (H + B)}$ $\bar{Y} = \frac{H^2 + B \cdot t}{2 \cdot (H + B)}$

Where:

I = Moment of inertia [mm<sup>4</sup>, in<sup>4</sup>]

$\bar{Y}$  = Center of Gravity Location [mm, in]

- a = Height fillet weld [mm, in]  
 B = Width of weld [mm, in]  
 s = Web thickness [mm, in]  
 L = Length of weld [mm, in]  
 r = Weld radius [mm, in]  
 t = Flange thickness [mm, in]  
 H = Height of fillet weld group [mm, in]

### Weld Design Menu

Weld	Throat Area of Fillet Weld A [mm <sup>2</sup> , in <sup>2</sup> ]	
	Full Weld Length	Active Load-bearing Length
	$A = a L$	$A = s (L - 2 a)$
	$A = a (H + B)$	$A = a (H + B - 2 a)$
	$A = a 2 H$	$A = a 2 (H - 2 a)$
	$A = a 2 B$	$A = a 2 (B - 2 a)$
	$A = a (H + 2 B)$	$A = a (H + 2 B - 2 a)$
	$A = a (2 H + B)$	$A = a (2 H + B - 2 a)$
	$A = a 2 (H + B)$	-
	$A = 2 \pi a (r + a / 2)$	-
	$A = a 2 (H + B)$ $A = a 2 (H + B - 2 t)$	$A = a 2 (H + B - 4 a)$ $A = a 2 (H + B - 2 t - 4 a)$
	$A = a 2 (H + 2 B)$ $A = a 2 (H + 2 B - s)$	-
	$A = a 2 (H + B)$ $A = a 2 (H + B - 2 t)$	$A = a 2 (H + B - 4 a)$ $A = a 2 (H + B - 2 t - 4 a)$

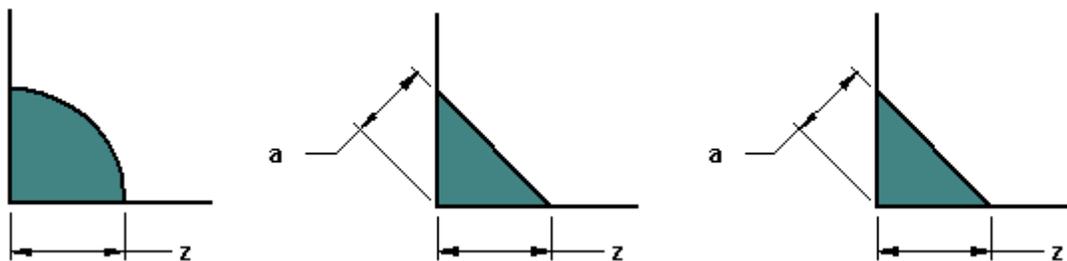
	$A = a^2 (2H + B)$ $A = a^2 (2H + B - s)$	-
	$A = a (2H + B)$ $A = a (2H + B - 2t)$	$A = a (2H + B - 6a)$ $A = a (2H + B - 2t - 6a)$
	$A = a^2 (H + B)$	-
	$A = a^2 L$	$A = a^2 (L - 2a)$

**Where:**

- A = Throat area of fillet weld [mm<sup>2</sup>, in<sup>2</sup>]
- B = Width of weld [mm, in]
- s = Web thickness [mm, in]
- L = Length of weld [mm, in]
- r = Weld radius [mm, in]
- t = Flange thickness [mm, in]
- H = Height of fillet weld [mm, in]

**Weld Design Menu**

The **active fillet weld height specification** is the largest isosceles triangle which may be inscribed with the theoretical weld cross-section.



The theoretical fillet weld size height approximately specifies  $a = .7z$  as given by trigonometry, where  $z$  is the fillet weld width. The minimum fillet weld height should be selected based on the actual thickness of the thickest weld part and the strength of the material.

Recommended Minimum Fillet Height Chart		
Thickest Welded Part	Minimum Fillet Weld Thickness [mm] fro Steel	
Over To	370 - 420	520 MPa

		MPa	
-	10	3	4
10	20	4	5
20	30	6	7
30	50	7	9
50		9	10

### Weld Design Menu

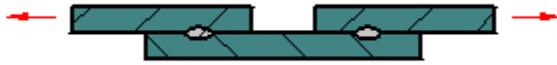
The following are recommended values for weld joint coefficient conversion.

Type of Weld	Loading	Coefficient of Weld joint			
butt <sup>1</sup>	Compression	$\alpha_1$	1.00		
	Tension		.85	.900 <sup>2</sup>	1.00 <sup>3</sup>
	Shear	$\alpha_2$	.70		
Fillet	End Load	$\alpha_3$	.75 <sup>4</sup>	.90 <sup>5</sup>	1.00 <sup>6</sup>
	Side	$\alpha_4$	.65 <sup>4</sup>	.80 <sup>5</sup>	.90 <sup>6</sup>
Groove and Plug	Shear	$\alpha$	.65		
Spot	Shear	$\alpha$	.65		
	Tear-out	$\alpha$	.5		

1. Coefficient of weld joint for loading along the axis of weld joint  $a = 1$
2. Contact resistance welding
3. Butt welds manually welded and supported by the weld from the root side after grooving butt welds bilaterally penetrated, automatic welding under flux or in CO<sub>2</sub> made at least from one side electro-slag welds
4. Manual arc welding while the strength of used electrode corresponds to the strength of basic material.
5. Applies to:
  - Manual arc welding of basic materials whose minimum tensile strength is 20 % lower than minimum strength of weld metal of used electrode
  - Semi-automatic submerged welding, semi-automatic and automatic welding shielded by CO<sub>2</sub> atmosphere and even for automatic submerged welding of single-pass or multi-pass welds for the weld height a 8 mm

6. Automatic submerged welding of single-pass welds for the weld height  $a < 8$  mm

7. [Weld Design Menu](#)



8.

9. Shear of Point

$$\tau_1 = \frac{4 \cdot F}{i \cdot \pi \cdot d^2} \quad [\text{MPa,psi}]$$

10.

11. Tear Loading of Point along Cylindrical Surface

$$\tau_2 = \frac{F}{i \cdot \pi \cdot d \cdot s} \quad [\text{MPa,psi}]$$

12.

13. Comparative Stress

$$\sigma_5 = \max \left\langle \frac{\tau_1}{\alpha}, \frac{\tau_2}{\alpha} \right\rangle \quad [\text{MPa,psi}]$$

14.

**Where:**

$\tau_1$  = Shear stress [MPa,psi]

$\tau_2$  = Tear stress [MPa,psi]

$\sigma_5$  = Comparative stress [MPa,psi]

F = Applied force [N, lb]

s = Thickness, plate [mm, in]

d = Spot weld diameter [mm, in]

i = Number of welds

$\alpha$  = Coefficient of weld joint

---

[Weld Design Menu](#)



**Shear of Point**

$$\tau_1 = \frac{2 \cdot F}{i \cdot \pi \cdot d^2} \quad [\text{MPa,psi}]$$

**Tear Loading of Point along Cylindrical Surface**

$$\tau_2 = \frac{F}{2 \cdot i \cdot \pi \cdot d \cdot s} \quad [\text{MPa, psi}]$$

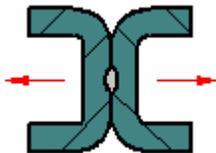
### Comparative Stress

$$\sigma_S = \max\left\langle \frac{\tau_1}{\alpha}, \frac{\tau_2}{\alpha} \right\rangle \quad [\text{MPa, psi}]$$

### Where:

- $\tau_1$  = Shear stress [MPa,psi]
- $\tau_2$  = Tear stress [MPa,psi]
- $\sigma_S$  = Comparative stress [MPa,psi]
- F = Applied force [N, lb]
- s = Thickness, plate [mm, in]
- d = Spot weld diameter [mm, in]
- i = Number of welds
- $\alpha$  = Coefficient of weld joint

### Weld Design Menu



### Tear-off Loading of Weld Area

$$\tau = \frac{4 \cdot F}{i \cdot \pi \cdot d^2} \quad [\text{MPa, psi}]$$

### Comparative Stress

$$\sigma_S = \frac{\tau}{\alpha} \quad [\text{MPa, psi}]$$

### Where:

- $\tau$  = Shear stress [MPa,psi]
- $\sigma_S$  = Comparative stress [MPa,psi]

- F = Applied force [N, lb]  
d = Spot weld diameter [mm, in]  
i = Number of welds  
 $\alpha$  = Coefficient of weld joint
- 
- 

## Introduction

The following notes are general guidance notes showing methods of calculation of the strength and size of welds. Welded joints are often crucially important affecting the safety of the design systems. It is important that the notes and data below are only used for preliminary design evaluations. Final detail design should be completed in a formal way using appropriate codes and standards and quality reference documents

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## Relevant Standards

BS 5950-1:2000 ..Structural use of steelwork in building. Code of practice for design. Rolled and welded sections

BS EN 10025-1:2004 - Hot rolled products of structural steels. General technical delivery conditions

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## Variables related to welded joints

1. Strength of deposited weld material
  2. Type of joint and weld..important
  3. Size of weld ..important
  4. Location of weld in relation to parts joined..important
  5. Types of stress to which the weld is subjected
  6. Conditions under which weld is carried out
  7. Type of equipment used for welding
  8. Skill of welder
- 

## Guidance Principles

A generous factor of safety should be used (3-5) and if fluctuating loads are present then additional design margins should be included to allow for fatigue

Use the minimum amount of filler material consistent with the job requirement

Try to design joint such that load path is not through the weld

The table below provides approximate stresses in, hopefully, a convenient way.

For the direct loading case the butt weld stresses are tensile/ compressive  $\sigma_t$  for the fillet welds the stresses are assumed to be shear  $\tau_s$  applied to the weld throat.

For butt welded joints subject to bending the butt weld stresses result from a tensile/compressive stress  $\sigma_b$  and a direct shear stress  $\tau_s$ .

In these cases the design basis stress should be  $\sigma_r = \text{Sqrt}(\sigma_b^2 + 4\tau_s^2)$

For Fillet welded joints subject to bending the stresses in the fillet welds are all shear stresses.

From bending  $\tau_b$  and from shear  $\tau_s$

In these cases the design basis stress is generally  $\tau_r = \text{Sqrt}(\tau_b^2 + \tau_s^2)$

The stresses from joints subject to torsion loading include shear stress from the applied load and shear stresses from the torque loading. The resulting stresses should be added vectorially taking care to choose the location of the highest stresses.

**Table of bracket weld subject to direct and bending stresses**

Method of Loading	Weldment	Stress in Weld $\sigma_b$ $\tau_s$ Weld size (h)	Weldment	Stress in Weld $\sigma_b$ $\tau_s$ Weld size (h)	Weldment	Stress in Weld $\tau_b$ $\tau_s$ Weld size (h)

	$\sigma_t = \frac{P}{b \cdot h}$ <p>Or</p> $h = \frac{P}{b \cdot \sigma_t}$		$\sigma_t = \frac{0,5 \cdot P}{b \cdot h}$ $h = \frac{0,5 \cdot P}{b \cdot \sigma_t}$		$\tau_s = \frac{0,71 \cdot P}{b \cdot h}$ $h = \frac{0,71 \cdot P}{b \cdot \tau_s}$
	$\sigma_b = \frac{6 \cdot P \cdot A}{b \cdot h^2}$ <p>Or</p> $\tau_d = \frac{P}{b \cdot h}$ $h = \sqrt{\frac{6 \cdot P \cdot A}{b \cdot \sigma_b}}$		$x = d^3 - (d-2h)^3$ $\sigma_b = \frac{6 \cdot P \cdot A \cdot d}{b \cdot x}$ $\tau_s = \frac{P}{2 \cdot b \cdot h}$		$x = (d+2h)^3 - d^3$ $\tau_b = \frac{8,5 \cdot P \cdot A \cdot (d+2h)}{b \cdot x}$ $\tau_s = \frac{0,71 \cdot P}{b \cdot h}$
	$\sigma_b = \frac{6 \cdot P \cdot A}{h \cdot d^2}$ $\tau_s = \frac{P}{d \cdot h}$ $h = \frac{6 \cdot P \cdot A}{\sigma_b \cdot d^2}$		$\sigma_b = \frac{3 \cdot P \cdot A}{h \cdot d^2}$ $\tau_s = \frac{P}{2 \cdot d \cdot h}$ $h = \frac{3 \cdot P \cdot A}{\sigma_b \cdot d^2}$		$\tau_b = \frac{4,26 \cdot P \cdot A}{b \cdot d^2}$ $\tau_s = \frac{0,71 \cdot P}{b \cdot d}$ $h = \frac{2,151 \cdot P \cdot A}{\tau_s \cdot d^2}$
			$x = (b-2h) \cdot (d-2h)$ $y = (b-2h) \cdot (d-2h)$ $\sigma_b = \frac{6 \cdot P \cdot A \cdot d}{b \cdot d^3 - x}$ $\tau_s = \frac{P}{(b \cdot d - y)}$		$x = (b+2h) \cdot (d+2h)$ $y = (b+2h) \cdot (d+2h)$ $\tau_b = \frac{8,49 \cdot P \cdot A \cdot d}{x \cdot b \cdot d^3}$ $\tau_s = \frac{1,41 \cdot P}{(y \cdot b \cdot d)}$

**Assessment of Fillet Weld Groups** ref notes and table [Properties of Fillet Welds as lines](#)

Important note: The methods described below is based on the simple method of calculation of weld stress as identified in BS 5950- clause 6.7.8.2 . The other method identified in BS 5950 - 1 clause 6.7.8.3 as the direction method uses the method of resolving the forces transmitted by unit

thickness welds per unit length into traverse forces ( $F_T$ ) and longitudinal forces ( $F_L$ ). I have, to some extent, illustrated this method in my examples below

The method of assessing fillet welds groups treating welds as lines is reasonably safe and conservative and is very convenient to use.

a) Weld subject to bending....See table below for typical unit areas and unit Moments of Inertia

A fillet weld subject to bending is easily assessed as follows.

1) The area of the fillet weld  $A_u$  (unit thickness) is calculated assuming the weld is one unit thick..

2) The (unit) Moment of Inertia  $I_u$  is calculated assuming the weld is one unit thick..

3) The maximum shear stress due to bending is determined..  $\tau_b = M.y/I_u$

4) The maximum shear stress due to direct shear is determined..  $\tau_s = P/A$

5) The resultant stress  $\tau_r = \text{Sqrt}(\tau_b^2 + \tau_s^2)$

6) By comparing the design strength  $p_w$  with the resultant stress  $\tau_r$  the value of the weld throat thickness is calculated and then the weld size.

i.e. if the  $\tau_r/p_w = 5$  then the throat thickness  $t = 5$  units and the weld leg size  $h = 1,414t$

a) Weld subject to torsion...See table below for typical unit areas and unit Polar moments of Inertia

A fillet weld subject to torsion is easily assessed as follows.

1) The area of the fillet weld  $A_u$  (unit thickness) is calculated assuming the weld is one unit thick

2) The (unit) Polar Moment of Inertia  $J_u$  is calculated assuming the weld is one unit thick.. The polar moment of inertia  $J = I_{xx} + I_{yy}$

3) The maximum shear stress due to torsion is determined..  $\tau_t = T.r/J_u$

4) The maximum shear stress due to direct shear is determined..  $\tau_s = P/A_u$

5) The resultant stress  $\tau_r$  is the vector sum of  $\tau_t$  and  $\tau_s$ .  $r$  is chosen to give the highest value of  $\tau_r$

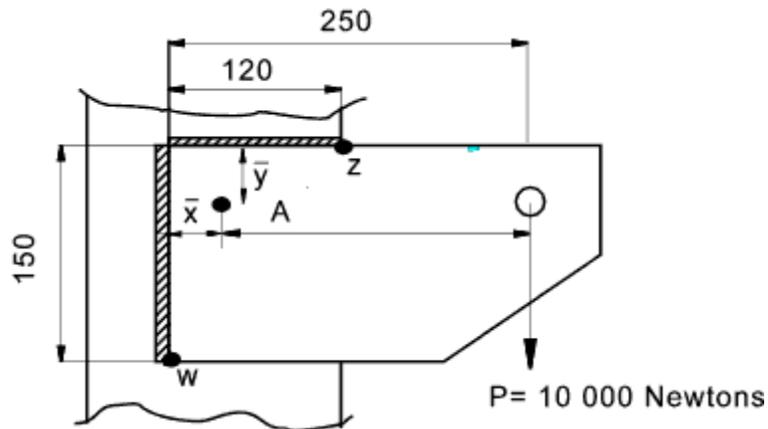
6) By comparing the design strength  $p_w$  with the resultant stress  $\tau_r$  the value of the weld throat thickness is calculated and then the weld size.

i.e. if the  $\tau_r/p_w = 5$  then the throat thickness  $t = 5$  units and the weld leg size  $h = 1,414.t$

---

### Examples of Fillet Weld Calculations

Example of Weld in Torsion..



$P =$  Applied load = 10 000N

$P_w =$  Design Strength = 220 N/mm<sup>2</sup> (Electrode E35 steel S275) [Design Strength](#)

$b =$  120mm.

$d =$  150 mm

$x = b^2 / 2(b+d) = 27\text{mm}..$  (From table below)

$y = d^2 / 2(b+d) = 42\text{mm}..$ (From table below)

#### Simple Method as BS 5950 clause 6.8.7.2

..The vector sum of the stresses due to forces and moments should not exceed the design strength

$P_w$

$A_u =$  Unit Throat Area

= (From table below)  $b + d = (120 + 150) = 270\text{mm}^2$

To obtain radius of Force from weld centre of gravity

$A = 250 - 27 = 223\text{mm}$

Moment  $M = P.r = 10000.223 = 2,23.10^6 \text{ N.mm}$

$J_u = [(b+d)^4 - 6b^2d^2] / 12 (b+d) = 1,04.10^6 ..$ (From Table)

It is necessary to locate the point subject to the highest shear stress..For a weld subject to only torsion this would be simply at the point furthest from the COG. However because the weld is subject to torsion and direct shear the problem is

#### Direction Method as BS 5950 clause 6.8.7.3

$L =$  Length of weld 1 unit thick =

(From table below)  $b + d = (120 + 150) = 270\text{mm}$

To obtain radius of Force from weld Centre of Gravity (Cog) .

$A = 250 - 27 = 223\text{mm}$

Moment  $M = P.r = 10000.223 = 2,23.10^6 \text{ N.mm}$

$J_u =$  Polar Moment of inertia for weld 1 unit(mm) thick.

=  $[(b+d)^4 - 6b^2d^2] / 12 (b+d) = 1,04.10^6 \text{ mm}^4 / \text{mm}..$ (From Table)

It is necessary to locate the point subject to the highest shear stress..For a weld subject to only torsion this would be simply at the point furthest from the COG. However because the weld is subject to torsion and direct shear the problem is more complicated. A normal method of determining the stresses in these cases is to use

more complicated. A normal method of determining the stresses in these cases is to use vector addition.

It is generally prudent to calculate the total shear stress at both positions, using the method below, and select the highest.. For this example the method used is to resolve the stresses in the x and y directions

---

First considering point Z

Horizontal distance from centroid  $r_{zh} = 120-27 = 93\text{mm}$

Vertical distance from centroid  $r_{zv} = 42\text{mm}$

The vertical stress  $\tau_v = \tau_{sv} + \tau_{tv}$

$$\tau_{sv} = P / A_u = 10000/270 = 37 \text{ N/mm}^2$$

$$\tau_{tv} = M.r_{zh} / J_u = 2,23.10^6.93/1,04.10^6 = 199 \text{ N/mm}^2$$

$$\tau_v = 236,45 \text{ N/mm}^2$$

The horizontal stress  $\tau_h = \tau_{sh} + \tau_{th}$

$$\tau_{sh} = 0$$

$$\tau_{th} = M.r_{zv} / J_u = 2,23.10^6.42/1,04.10^6 = 90 \text{ N/mm}^2$$

$$\tau_h = 90 \text{ N/mm}^2$$

The resultant stress on the weld at z

$$\tau_r = \text{Sqrt}(\tau_h^2 + \tau_v^2) = 253 \text{ N/mm}^2$$

---

Now considering point w

Horizontal distance from centroid  $r_{wh} = 27\text{mm}$

Vertical distance from centroid  $r_{wv} = 150-42 = 108\text{mm}$

The vertical stress  $\tau_v = \tau_{sv} - \tau_{tv}$

$$\tau_{sv} = P / A_u = 10000/270 = 37 \text{ N/mm}^2$$

vector addition.

It is generally prudent to calculate the total shear stress at both positions, using the method below, and select the highest.. For this example the method used is to resolve the stresses in the x and y directions

---

First considering point Z

Horizontal distance from centroid  $r_{zh} = 120-27 = 93\text{mm}$

Vertical distance from centroid  $r_{zv} = 42\text{mm}$

The vertical force /mm run  $F_v = F_{sv} + F_{tv}$

$$F_{sv} = P / L = 10000/270 = 37 \text{ N/mm run}$$

$$F_{tv} = M.r_{zh} / J_u = 2,23.10^6.93/1,04.10^6 = 199 \text{ N/mm run}$$

$$F_v = 236,45 \text{ N/mm run}$$

The horizontal force /mm run for unit(mm) weld width  $F_h = F_{sh} + F_{th}$

$$F_{sh} = 0$$

$$F_{th} = M.r_{zv} / J_u = 2,23.10^6.42/1,04.10^6 = 90 \text{ N/mm run}$$

$$F_h = 90 \text{ N/mm run}$$

The resultant force on the weld/mm run at z

$$F_r = \text{Sqrt}(F_h^2 + F_v^2) = 253 \text{ N/mm run}$$

---

Now considering point w

Horizontal distance from centroid  $r_{wh} = 27\text{mm}$

Vertical distance from centroid  $r_{wv} = 150-42 = 108\text{mm}$

The vertical forces per mm run  $F_v = F_{sv} - F_{tv}$

$$F_{sv} = P / L = 10000/270 = 37 \text{ N/mm run}$$

$$\tau_{tv} = M.r_{wh} / J_u = 2,23.10^6 .27 / 1,04.10^6 = 57,9 \text{ N/mm}^2$$

$$\tau_v = 20,86 \text{ N/mm}^2$$

The horizontal stress  $\tau_h = \tau_{sh} + \tau_{th}$

$$\tau_{sh} = 0$$

$$\tau_{th} = T.r_{wv} / J_u = 2,23.10^6 .108 / 1,04.10^6 = 231,6 \text{ N/mm}^2$$

$$\tau_h = 231,6 \text{ N/mm}^2$$

The resultant stress on the weld at w

$$\tau_r = \text{Sqrt}(\tau_h^2 + \tau_v^2) = 232,5 \text{ N/mm}^2$$

The maximum stress is similar but greatest at z ....

The design strength  $p_w$  for the weld material is 220 N/mm<sub>2</sub>

The weld throat thickness should be  $253 / 220 = 1,15\text{mm}$  .

The weld size is therefore  $1,414 . 1,15 = 1,62\text{mm}$   
use 3mm fillet weld

$$F_{tv} = M.r_{wh} / J_u = 2,23.10^6 .27 / 1,04.10^6 = 57,9 \text{ N/mm run}$$

$$F_v = 20,86 \text{ N/mm run}$$

The horizontal force /mm run =  $F_h = F_{sh} + F_{th}$

$$F_{sh} = 0$$

$$F_{th} = M.r_{wv} / J_u = 2,23.10^6 .108 / 1,04.10^6 = 231,6 \text{ N/mm run}$$

$$F_h = 231,6 \text{ N/mm run}$$

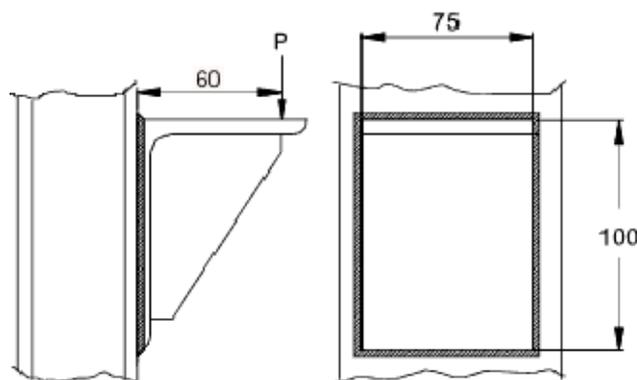
The specific force on the weld at w

$$F_r = \text{Sqrt}(F_h^2 + F_v^2) = 232,5 \text{ N/mm run}$$

The maximum specific is greatest at z = 253 N/mm run....

Referring to weld capacities for longitudinal stresses  $P_L$  for fillet welds [Capacities of Fillet Welds](#) the weld capacity for a 3mm weld with and E35 Electrode S275 Steel is 462N /mm run. This weld would be more than sufficient.

### Example of Weld in Bending..



P= 30000 Newtons

d= 100mm

b= 75mm

y = 50mm

Design Stress  $p_w = 220 \text{ N/mm}^2$  (Electrode E35 steel S275) [Design Strength](#)

Moment =  $M = 30000 \cdot 60 = 18.10^5 \text{ Nmm}$

### Simple Method as BS 5950 clause 6.8.7.2

Unit Weld Area =  $A_u = 2(d+b) = 2(100+75) = 350 \text{ mm}^2$

Unit Moment of Inertia =  $I_u$   
 $= d^2(3b+d) / 6 = 100^2 (3 \cdot 75 + 100) / 6 = 5,42 \cdot 10^5 \text{ mm}^4$

$$\tau_r = \text{Sqrt}(\tau_s^2 + \tau_b^2)$$

$$\tau_s = P / A_u = 30000 / 350 = 85,71 \text{ N/mm}^2$$

$$\tau_b = M \cdot y / I_u = 18.10^5 \cdot 50 / 5,42 \cdot 10^5 = 166,05 \text{ N/mm}^2$$

$$\tau_r = \text{Sqrt}(85,71^2 + 166,05^2) = 186,86 \text{ N/mm}^2$$

$$\tau_r / p_w = 186,86 / 220 = 0,85 = \text{Throat Thickness} \dots$$

( Throat thickness for  $\tau = 220 \text{ N/mm}^2$  )

Leg Length = Throat thickness \* 1,414 = 1,2mm use  
3mm weld thickness

Note : If a leg length  $h = 1,2 \text{ mm}$  is used in the equations in relevant part of the "Table of bracket weld subject to direct and bending stresses" above a value of  $\tau_b = 198 \text{ N/mm}$  and a value of  $\tau_s = 100 \text{ N/mm}^2$  results with a resultant stress of  $\text{Sqrt}(\tau_b^2 + \tau_s^2) = 222 \text{ N/mm}^2$ . Which is in general agreement with the above result

### Direction Method as BS 5950 clause 6.8.7.3

Length of Weld of unit thickness =  $L = 2(d+b) = 2(100+75) = 350 \text{ mm}$

Moment of Inertia / mm throat thickness =  $I_u$  / mm

$$= d^2(3b+d) / 6 = 100^2 (3 \cdot 75 + 100) / 6 = 5,42 \cdot 10^5 \text{ mm}^4 / \text{mm}$$

$F_r$  = Resultant force per unit length of weld.

$F_s$  = Shear force per unit length of weld.

$F_b$  = Bending force per unit length of weld.

$$F_r = \text{Sqrt}(F_s^2 + F_b^2)$$

$F_s = P / L = 30000 / 350 = 85,71 \text{ N per mm length of weld}$

$$F_b = M \cdot y / I_u$$

$$= 18.10^5 \cdot 50 / 5,42 \cdot 10^5 = 166,05 \text{ N per mm length of weld}$$

$F_r = \text{Sqrt}(85,71^2 + 166,05^2) = 186,86 \text{ N per mm length of weld.}$

For this case for the welds under greatest loading the type of loading is traverse loading. The bending stress is in line with horizontal element and the shear stress is in line with vertical member.

The angle of the resulting specific load to the horizontal element

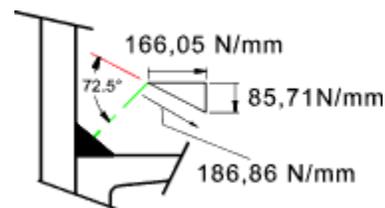
$$= \arctan(85,71/166,5) = 27,5^\circ$$

This is an angle with the weld throat  $\theta = 45^\circ + 27,5^\circ = 72,5^\circ$  Referring to weld capacities table below. [Weld Capacities](#) K is calculated at 1,36 for this resultant direction of forces.

$P_T = a \cdot K \cdot p_w$  for a E35 Weld electrode used with S275 steel

$p_w = 220 \text{ N/mm}^2$  and therefore  $P_T = a \cdot 300 \text{ N/mm}^2$ .

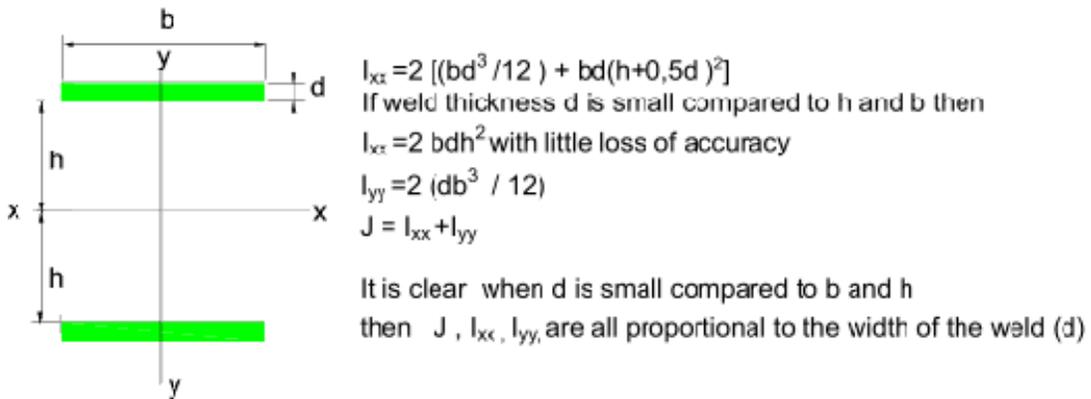
A 3mm weld ( $a = 2,1 \text{ mm}$ ) therefore will therefore have a design capacity of 630 N/mm run and will easily be able to support the load of 186,86 N per mm run



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### Properties of weld groups with welds treated as lines -

It is accepted that it is reasonably accurate to use properties based on unit weld thickness in calculation to determine the strength of welds as shown in the examples on this page. The weld properties  $I_{xx}$ ,  $I_{yy}$  and  $J$  are assumed to be proportional to the weld thickness. The typical accuracy of this method of calculation is shown below...

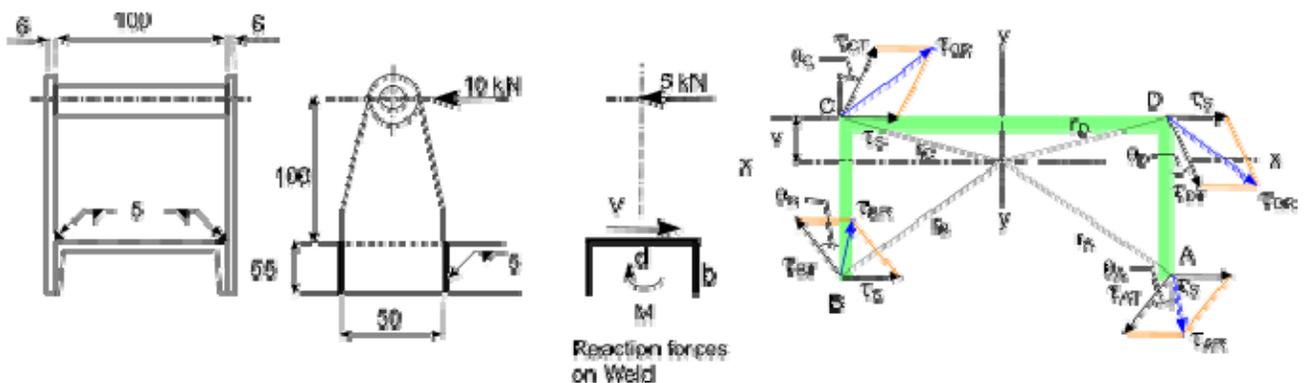


This is illustrated in the tabled values below

	d	b	h	$I_{xx}$	$I_{yy}$	$J = I_{xx} + I_{yy}$
Accurate	3	60	50	955080	108000	1063080
Simple	3	60	50	900000	108000	1008000
Error				6%	0	5%

Note: The error identified with this method is lower as  $h$  increases relative to  $d$ . This error is such that the resulting designs are conservative.

### Example illustrating use of stress vectors



**Calculation based on real weld sizes**

1) The area of the welds  
(based on throat weld thickness at 0,707.5 = 3,5mm)

$$\text{Area} = (57.3,5 + 2.55.3,5) = 584,5\text{mm}^2$$

2) The moment of area about x-x =

$$\text{M of Area} = (57.3,5.3,5/2 + 2.55.3,5.(27,5 + 3,5)) = 12\,284\text{mm}^3$$

3) The centroid  $v = \text{Moment of Area}/\text{Area}$

$$\text{M of Area} / \text{Area} = 21 \text{ mm}$$

4) The radii  $r_A, r_B, r_C$  &  $r_D$  are calculated ..

$$r_A = r_B = \text{Sqrt}((58,5-21)^2 + 28,5^2) = 47,1$$

$$r_C = r_D = \text{Sqrt}((21)^2 + 28,5^2) = 35,40\dots$$

5) The angles  $\theta_A, \theta_B, \theta_C$  &  $\theta_D$  are calculated ..

$$\theta_A = \theta_B = \tan^{-1}((58,5-21)/28,5) = 52,7^\circ$$

$$\theta_C = \theta_D = \tan^{-1}(21/28,5) = 36,4^\circ\dots$$

6) The direct shear stress on the area = Force /Area

$$\tau_s = 5000/584 = 8,56 \text{ N/mm}^2$$

7) The Moment on the weld group = Force.Distance to centroid

$$M = 5000.(100+21) = 6,05.10^5\text{Nmm}$$

8) The polar moment of inertia of the weld group =  $J = I_{xx} + I_{yy}$

$$I_{yy} = 2.[55.3,5^3/12 + 3,5.55.(50/2 + 3,5/2)^2] + 57^3.3,5/12 = 3,3.10^5\text{mm}^4$$

$$I_{xx} = 2.[55^3.3,5/12 + 3,5.55.(55/2 + 3,5 - 21)^2] + 3,5^3.57/12 + 3,5.57.(21-3,5/2)^2 = 2,097.10^5\text{mm}^4$$

**Calculations based on unit values**

This calculation uses equations from table below for Area, centroid, and  $J_u$

1) Area of weld = 0,707.5.(2b+d)

$$\text{Area} = 0,707.5.(2.55 + 50) = 565.6\text{mm}^2$$

2) There is no need to calculate the Moment of Area with this method

3) The centroid  $v = b^2/(2b+d)$

$$v = 55^2/(2.55+50) = 18,9\text{mm}$$

4) The radii  $r_A, r_B, r_C$  &  $r_D$  are calculated ..

$$r_A = r_B = \text{Sqrt}((55-18,9)^2 + 25^2) = 43,9$$

$$r_C = r_D = \text{Sqrt}(18,9^2 + 25^2) = 31,34$$

5) The angles  $\theta_A, \theta_B, \theta_C$  &  $\theta_D$  are calculated ..

$$\theta_A = \theta_B = \tan^{-1}((55-18,9)/25) = 55,29^\circ$$

$$\theta_C = \theta_D = \tan^{-1}(18,9/25) = 37^\circ\dots$$

6) The direct shear stress on the area = Force /Area

$$\tau_s = 5000/565,5 = 8,84 \text{ N/mm}^2$$

7) The Moment on the weld group = Force .distance to centroid

$$M = 5000.(100+18,9) = 5.94.10^5\text{Nmm}$$

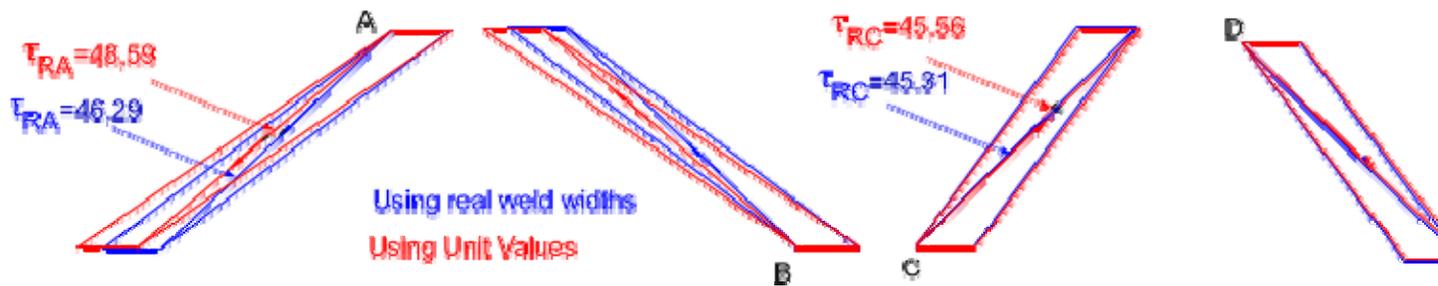
8) The Unit Polar moment of inertia of the weld group =

$$J_u = 0.707.5.(8.b^3 + 6bd^2 + d^3)/12 + b^4/(2b+d)$$

$$J_u = 0,707.5.(8.55^3 + 6.55.50^2 + 50^3)/12 - 55^3/(2.55+50) = 4,69.10^5$$

9) The stress due to torsion

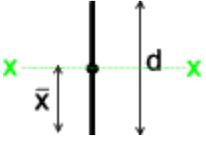
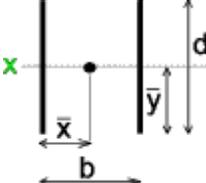
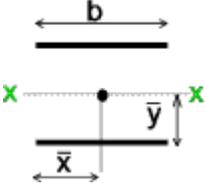
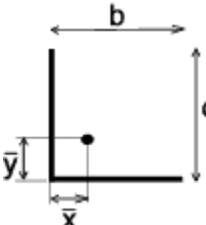
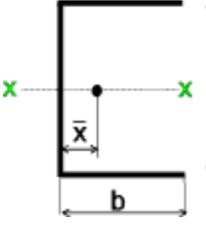
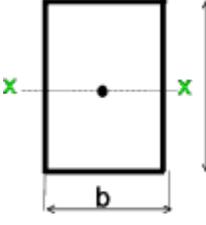
$J = I_{xx} + I_{yy} = 5,4 \cdot 10^5 \text{mm}^4$ <p>9) The stress due to torsion  <math>\tau_{TA} = \tau_{TB} = M \cdot r_A / J</math> and <math>\tau_{TC} = \tau_{TD} = M \cdot r_C / J</math>  <math>\tau_{TA} = 6,05^5 \text{Nmm} \cdot 47,1 \text{mm} / 5,4 \cdot 10^5 \text{mm}^4 = 52,8 \text{N/mm}^2</math>  <math>\tau_{TC} = \tau_{TD} = 6,05^5 \text{Nmm} \cdot 35,4 \text{mm} / 5,4 \cdot 10^5 \text{mm}^4 = 39,70 \text{N/mm}^2</math></p> <p>10) The resultant stresses <math>\tau_{RA}, = \tau_{RB}</math> and <math>\tau_{RA}, = \tau_{RB}</math> are obtained by adding the stress vectors graphically as shown below</p> $\tau_{RA} = \tau_{RB} = 46,29 \text{N/mm}^2$ $\tau_{RC} = \tau_{RD} = 45,31 \text{N/mm}^2$	$\tau_{TA} = \tau_{TB} = M \cdot r_A / J$ and $\tau_{TC} = \tau_{TD} = M \cdot r_C / J$ $\tau_{TA} = 5,94 \cdot 10^5 \text{Nmm} \cdot 43,9 \text{mm} / 4,69 \cdot 10^5 \text{mm}^4 = 55,6 \text{N/mm}^2$ $\tau_{TC} = \tau_{TD} = 5,94^5 \text{Nmm} \cdot 31,34 \text{mm} / 4,69 \cdot 10^5 \text{mm}^4 = 39,69 \text{N/mm}^2$ <p>10) The resultant stresses <math>\tau_{RA}, = \tau_{RB}</math> and <math>\tau_{RA}, = \tau_{RB}</math> are obtained by adding the stress vectors graphically as shown below</p> $\tau_{RA} = \tau_{RB} = 48,59 \text{N/mm}^2$ $\tau_{RC} = \tau_{RD} = 45,56 \text{N/mm}^2$
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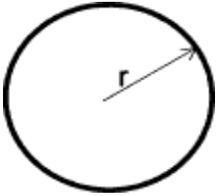


Note: The example above simply illustrates the vector method adding direct and torsional shear stresses and compares the difference in using the unit weld width method and using real weld sizes. The example calculates the stress levels in an existing weld group it is clear that the weld is oversized for the loading scenario. The difference in the resulting values are in less than 4%. If the welds were smaller i.e 3mm then the differences would be even smaller.

Table properties of a range of fillet weld groups with welds treated as lines -

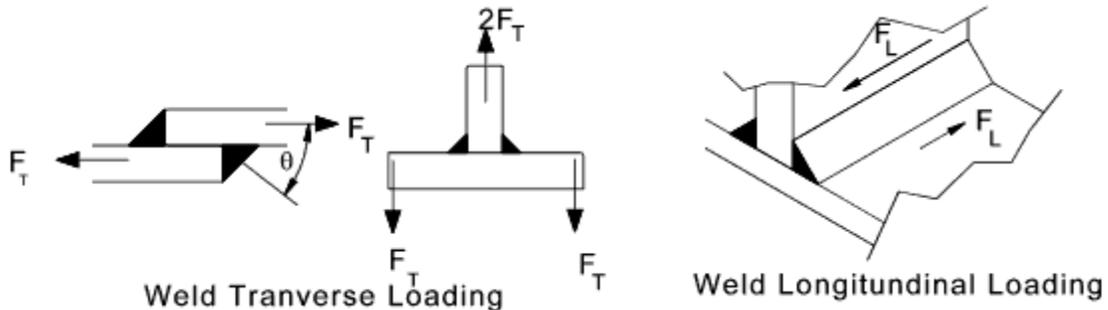
Weld	Throat Area Unit Area	Location of COG x y	$I_{xx}$ -(unit)	J-(Unit)

	$0,707hd$ $d$	$\bar{x} = 0$ $\bar{y} = d / 2$	$I_{xx} = \frac{d^3}{12}$	$J = \frac{d^3}{12}$
	$1,414hd$ $2d$	$\bar{x} = b/2$ $\bar{y} = d/2$	$I_{xx} = \frac{d^3}{6}$	$J = \frac{d(3b^2 + d^2)}{6}$
	$1,414hb$ $2.b$	$\bar{x} = b/2$ $\bar{y} = d/2$	$I_{xx} = \frac{bd^2}{2}$	$J = \frac{b(3d^2 + b^2)}{6}$
	$0,707 h (b+d)$ $b + d$	$\bar{x} = \frac{b^2}{2(b+d)}$ $\bar{y} = \frac{d^2}{2(b+d)}$	-	$J = \frac{(b+d)^4 - 6b^2 d^2}{12(b+d)}$
	$0,707h(2b+d)$ $2b + d$	$\bar{x} = b^2/(2b+d)$ $\bar{y} = d/2$	$I_{xx} = \frac{d^2(6b + d)}{12}$	$z = 8b^3 + 6bd^2 + d^3$ $J = \frac{z}{12} - \frac{b^4}{2b+d}$
	$1,414 h(b+d)$ $2(b + d)$	$\bar{x} = b/2$ $\bar{y} = d/2$	$I_{xx} = \frac{d^2(3b + d)}{6}$	$J = \frac{(b+d)^3}{6}$

	$1,414 \pi r$ $2\pi r$	-	$I = \pi r^3$	$J = 2\pi r^3$
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### Table Of Weld Capacities

The fillet weld capacity tables related to the type of loading on the weld. Two types of loading are identified traverse loading and longitudinal loading as show below



The weld loading should be such that

$$\{ (F_L/P_L)^2 + (F_T/P_T)^2 \} \leq 1$$

The following table is in accord with data in BS 5950 part 1. Based on design strengths as shown in table below ... [Design Strength](#)

$$P_L = a.p_w$$

$$P_T = a.K.p_w$$

a = weld throat size.

$$K = 1,25 \sqrt{1,5 / (1 + \text{Cos}^2 \theta)}$$

$P_T$  based on elements transmitting forces at  $90^\circ$  i.e  $\theta = 45^\circ$  and  $K = 1,25$

Weld Capacity E35 Electrode S275 Steel				Weld Capacity E42 Electrode S355 Steel			
Leg	Throat	Longitudinal	Transverse	Leg	Throat	Longitudinal	Transverse

Length	Thickness	Capacity	Capacity	Length	Thickness	Capacity	Capacity
		$P_L$ (kN/mm)	$P_T$ (kN/mm)			$P_L$	$P_T$
mm	mm	kN/mm	kN/mm	mm	mm	kN/mm	kN/mm
3	2,1	0,462	0,577	3	2,1	0,525	0,656
4	2,8	0,616	0,720	4	2,8	0,700	0,875
5	3,5	0,770	0,963	5	3,5	0,875	1,094
6	4,2	0,924	1,155	6	4,2	1,050	1,312
8	5,6	1,232	1,540	8	5,6	1,400	1,750
10	7,0	1,540	1,925	10	7,0	1,750	2,188
12	8,4	1,848	2,310	12	8,4	2,100	2,625
15	10,5	2,310	2,888	15	10,5	2,625	3,281
18	12,6	2,772	3,465	18	12,6	3,150	3,938
20	14,0	3,08	3,850	20	14,0	3,500	4,375
22	15,4	3,388	4,235	22	15,4	3,850	4,813
25	17,5	3,850	4,813	25	17,5	4,375	5,469

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**Design Strength  $p_w$  of fillet welds**

	Electrode classification
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Steel Grade	35	43	50
	N/mm <sup>2</sup>	N/mm <sup>2</sup>	N/mm <sup>2</sup>
S275	220	220	220
S355	220	250	250
S460	220	250	280